

GOODNESS OF FIT

| How to tell it's Goodness of Fit |
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| <ul style="list-style-type: none"> There is only 1 variable There are old/known values & new observed values |

| Hypotheses | | | |
|------------|------------------------------|-------|-------------------------------------|
| H_0 | The proportions are correct. | H_1 | At least 1 proportion is incorrect. |



| Math Time! | |
|--------------------|---|
| Expected Counts | $E_i = n \cdot p_i$ |
| Test Statistic | $\chi^2 = TS = \sum \left(\frac{(O_i - E_i)^2}{E_i} \right)$ |
| Degrees of Freedom | $df = \#categories - 1$ |
| P-value | $p = \chi^2_{cdf}(TS, eqn, df)$ |



| Decision and Interpretation | |
|--|--|
| Rejecting Null ($\alpha > p$) | There is sufficient evidence to say that at least 1 proportion is incorrect. |
| Failing to Reject Null ($\alpha < p$) | There is insufficient evidence to say that at least 1 proportion is incorrect. |

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| Calculator Trick (χ^2 GOF-Test) |
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|--------------------------|--|
| How do you get there? | STAT → TESTS → D: χ^2 GOF-Test |
| What do you need for it? | <ul style="list-style-type: none"> • Observed Counts in list • Expected Counts in list • Degrees of Freedom |
| What do you get from it? | • TS → χ^2 • p-value • Df |

TEST OF INDEPENDENCE & TEST OF HOMOGENEITY

| How to tell it's... | |
|--|--|
| Test of Independence | Test of Homogeneity |
| <ul style="list-style-type: none"> • There are 2 variables • Question has words like 'relationship' or 'association' | <ul style="list-style-type: none"> • There are 2 variables • Question has phrases like 'the same' or 'are equal' |

| Hypotheses | | | |
|----------------------|-------------------------------|---------------------|--|
| Test of Independence | | Test of Homogeneity | |
| H_0 | The variables are independent | H_0 | The distributions are equal/the same |
| H_1 | The variables are dependent | H_1 | The distributions are unequal/not the same |



| Math Time! | |
|--|--|
| Find Row/Column Totals & Overall Total | *Note: Overall total is found by adding row totals OR column totals |
| Expected Counts | $E_{i,j} = \frac{(\text{i}^{\text{th}} \text{ row total})(\text{j}^{\text{th}} \text{ column total})}{\text{Overall total}}$ |
| Test Statistic | $\chi^2 = TS = \sum \left(\frac{(O_{i,j} - E_{i,j})^2}{E_{i,j}} \right)$ |

| | |
|--------------------|---|
| Degrees of Freedom | $df = (\#rows - 1)(\#columns - 1)$ |
| P-value | $p = \chi^2_{cdf}(TS, \epsilon_{99}, df)$ |



| Decision and Interpretation | | |
|--|-----|---|
| Rejecting Null ($\alpha > p$) | TOI | There is sufficient evidence to say that the variables are dependent of each other. |
| | TOH | There is sufficient evidence to say that the distributions are unequal. |
| Failing to Reject Null ($\alpha < p$) | TOI | There is insufficient evidence to say that the variables are dependent of each other. |
| | TOH | There is insufficient evidence to say that the distributions are unequal. |

| Calculator Trick | |
|--------------------------|--|
| Part 1: The Matrix | |
| How do you get there? | 2nd \rightarrow χ^{-1} \rightarrow Edit \rightarrow Pick one |
| What do you need for it? | Observed Counts |
| Part 2: χ^2 -Test | |
| How do you get there? | STAT \rightarrow TESTS \rightarrow C: χ^2 -Test |
| What do you need for it? | <ul style="list-style-type: none"> • Observed Count Matrix • Empty Matrix for Expected Counts |
| What do you get from it? | <ul style="list-style-type: none"> • Expected Counts • $TS = \chi^2$ • p-value • df |

ANOVA

| How to tell it's ANOVA |
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| <ul style="list-style-type: none"> • There is only 1 variable • Question often has phrases like 'most', 'least', or 'different' when discussing the levels of the variable |

| Hypotheses | | | |
|------------|---------------------------------|-------|-------------------------|
| H_0 | $\mu_1 = \mu_2 = \dots = \mu_T$ | H_1 | At least 1 mean differs |



| Math Time! | | |
|--------------------|--|--------------------------------|
| | Between | Within |
| Sum of Squares | $SSB = \sum (n_i (\bar{x}_i - \bar{x})^2)$ | $SSW = \sum ((n_i - 1) s_i^2)$ |
| Degrees of Freedom | $df_B = T - 1$ | $df_W = n - T$ |
| Mean of Squares | $MSB = \frac{SSB}{df_B}$ | $MSW = \frac{SSW}{df_W}$ |
| Test Statistic | $F = TS = \frac{MSB}{MSW}$ | |
| P-value | $p = Fcdf(TS, E49, df_B, df_W)$ | |



| Decision and Interpretation | |
|------------------------------------|---|
| Rejecting Null ($\alpha > p$) | There is sufficient evidence to say that at least 1 mean differs. |
| | |

| | |
|--|---|
| Failing to Reject Null ($\alpha < p$) | There is insufficient evidence to say that at least 1 mean differs. |
|--|---|

| Calculator Trick (ANOVA) | |
|--------------------------|---|
| How do you get there? | STAT \rightarrow TESTS \rightarrow H: ANOVA(|
| What do you need for it? | All the levels' data in lists |
| What do you get from it? | <ul style="list-style-type: none"> • F=TS • p-value • Factor Stats \rightarrow Between Values • Error Stats \rightarrow Within Values |

POST-HOC

| How to tell it's Post-Hoc |
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| <ul style="list-style-type: none"> • Question asks something along the line of which mean differs from the rest |
| *Note: Only use when you <u>REJECT NULL</u> on ANOVA! |

Suppose there are 3 μ

| Hypotheses | | | |
|------------|---|-------|--|
| H_0 | $\mu_1 = \mu_2 ; \mu_1 = \mu_3 ; \mu_2 = \mu_3$ | H_1 | $\mu_1 \neq \mu_2 ; \mu_1 \neq \mu_3 ; \mu_2 \neq \mu_3$ |



| Decision and Interpretation for Each Comparison | |
|---|--------------------------|
| Rejecting Null ($\alpha > p$) | $\mu_{\#} \neq \mu_{\#}$ |
| Failing to Reject Null ($\alpha < p$) | $\mu_{\#} = \mu_{\#}$ |



Interpretation Overall

There is sufficient evidence to say that the mean of _____ are different from _____.

* Honestly, just write/chose what you see in your analysis of the R code you are provided.