

Theory Recap

- A numerical measure of a population is known as population parameter
 - This uses ALL the values of a population
- A numerical descriptive measure of a sample is known as sample statistic
 - Found in calculations using observations from experiments
- The probability distribution of the statistics constructed from many samples of the same size is known as the sampling distribution

	Population Parameter	Sample Statistic
Mean	μ	\bar{X}
Median	η	M or Q_2
Variance	σ^2	s^2
Standard Deviation	σ	s
Binomial Proportion	p	\hat{p}

- A number that is calculated from a sample to estimate the target parameter is known as the Point Estimate
- The interval of numbers calculated from a sample that contains the target parameter is known as the Confidence Interval
- The probability that the estimation method will generate a Confidence Interval is known as the Confidence Level
 - The most common values used are: 99%, 95%, 90%
- The complement of the Confidence Level is known as the Type I Error (α)
 - To find this, we use: $\alpha = 1 - (\text{Confidence Level})$
 - The most common values used are: 10%, 5%, 10%
 - If you are not given one in the question, we assume that it is 5%
- The overall formula for finding Confidence Interval is...

(Point Estimate - Margin of Error, Point Estimate + Margin of Error)

95% Confidence
Level
↑

Population Mean Theory

- The way we solve for the confidence interval depends on the sample size.
 - Considered large if the total (n) is $n \geq 30$ and small if the total (n) is $n < 30$.

- Formulas to understand:

- Point Estimate (For large and small sizes)

$$PE = \bar{X} = \frac{\sum X}{n}$$

- Margin of Error

- For large samples

$$MOE = Z_{\alpha/2} \frac{s}{\sqrt{n}}$$

- For small samples

$$MOE = t_{\alpha/2} \frac{s}{\sqrt{n}}$$

- Critical Value

- For large samples ($Z_{\alpha/2}$)

$$Z_{\alpha/2} = \left| \text{invNorm}\left(\frac{\alpha}{2}, \mu, \sigma\right) \right|$$

- For small samples ($t_{\alpha/2}$)

$$t_{\alpha/2} = \left| \text{invT}\left(\frac{\alpha}{2}, df\right) \right|$$

- T-distribution

- Very similar to normal distribution except it works with a family or multiple of distributions instead of a single distribution.

- Uses degrees of freedom

- $df = n - 1$

- Interpretation

We are % confidence that the true unknown population mean lies in the interval (solved confidence interval).

- Calculator Tricks for Population Mean C.I.

- o For large samples

- ZInterval

Stat --> Tests --> 7: ZInterval

- o For small samples

- TInterval

Stat --> Tests --> TInterval

- o Regardless of which trick you have to use, there are two paths in using the function:

- Data

- Use lists after the data is entered into the calculator
 - Also need the confidence level

- Stats

- Need: mean (μ), standard deviation (σ), and sample size (n)
 - Also need the confidence level